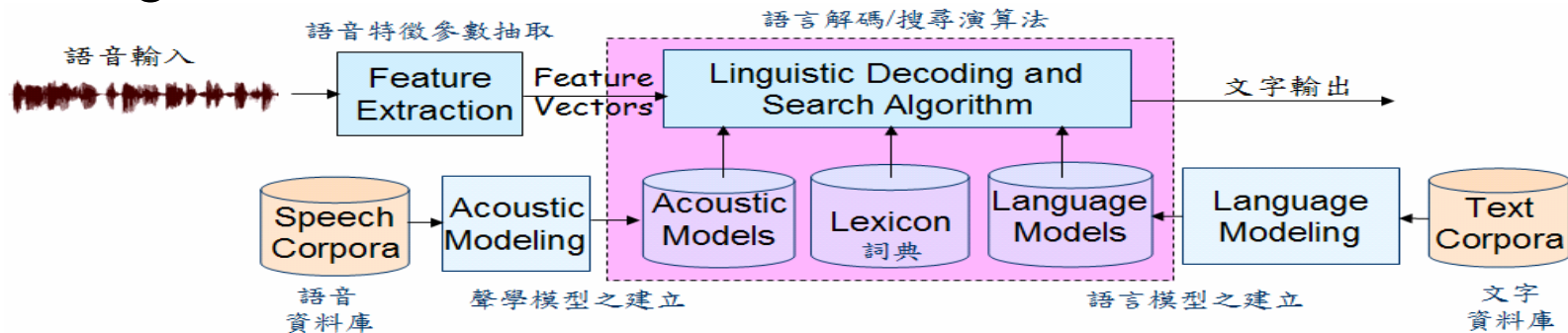


Large Vocabulary Continuous Speech Recognition

Berlin Chen 2003

Why LVCSR Difficult ?

- The software complexity of a search algorithm is considerable
- The effort required to build an efficient decoder is quite large

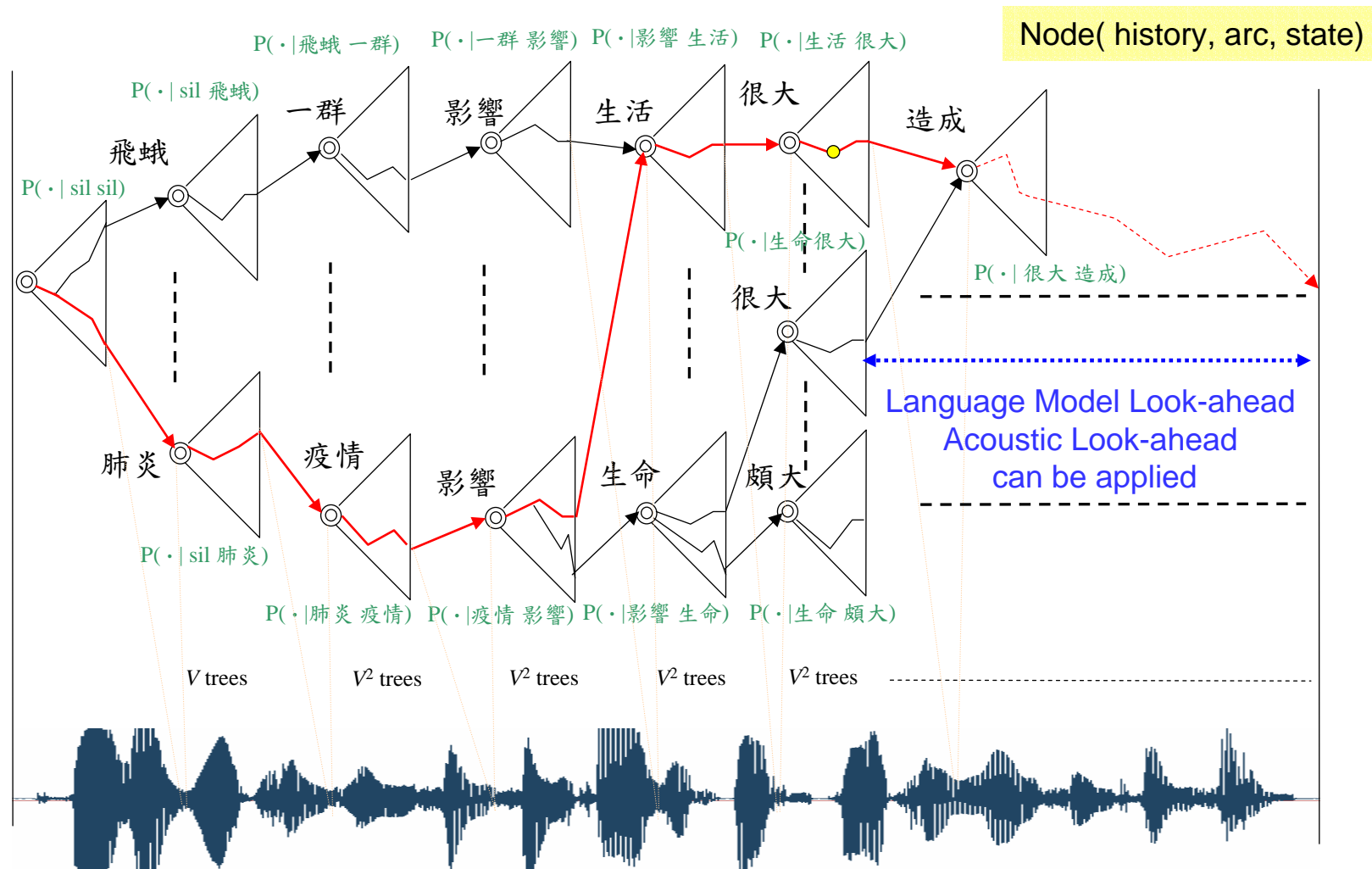


$$\begin{aligned}
 \hat{W} &= \arg \max_W P(W | X) \\
 &= \arg \max_W \frac{P(X | W)P(W)}{P(X)} \\
 &= \arg \max_W P(X | W)P(W)
 \end{aligned}$$

可能詞句 (Possible words) → \hat{W}
 語音輸入 (Speech input) → X
 貝氏定理 (Bayes' theorem) → $P(W | X) = \frac{P(X | W)P(W)}{P(X)}$
 詞彙網路搜尋 (Lexicon network search) → $P(W)$
 聲學模型機率 (Acoustic model probability) → $P(X | W)$
 語言模型機率 (Language model probability) → $P(W)$

One-Pass Tree-Copy Search

- Trigram language modeling used here

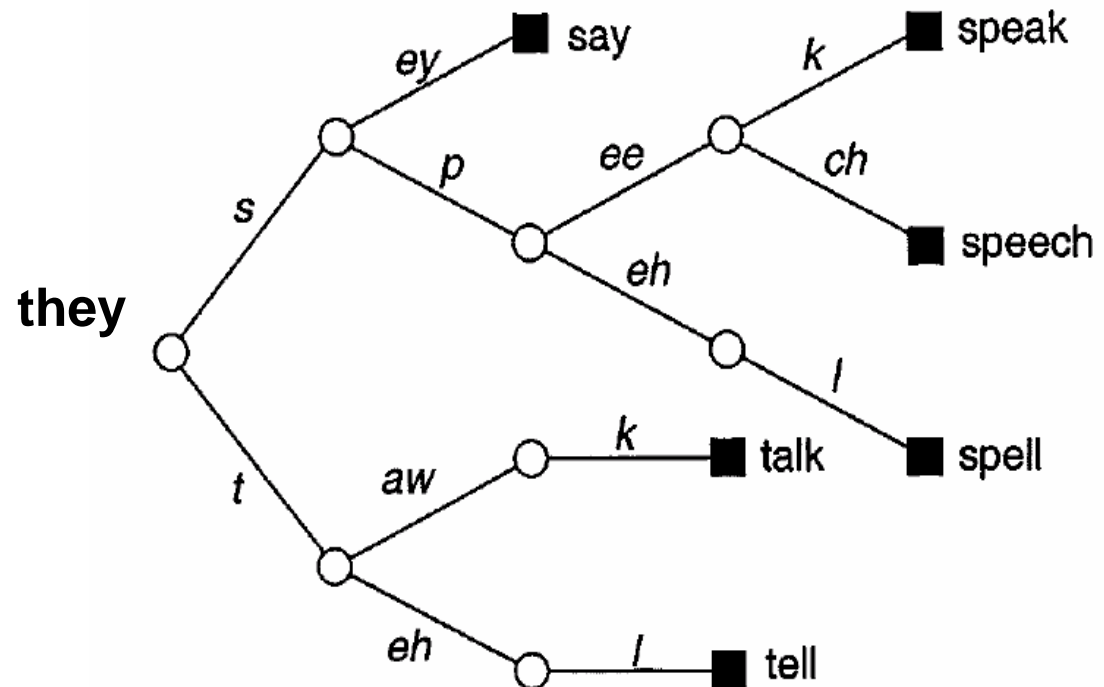


Lexical/Phonetic Tree

- Each arc stands for a phonetic unit
- Each leaf node is shared by words having the same pronunciation
- The application of language modeling is delayed until leaf nodes are reached

$$P(\textit{say} | \textit{they})$$

$$P(\textit{tell} | \textit{they})$$

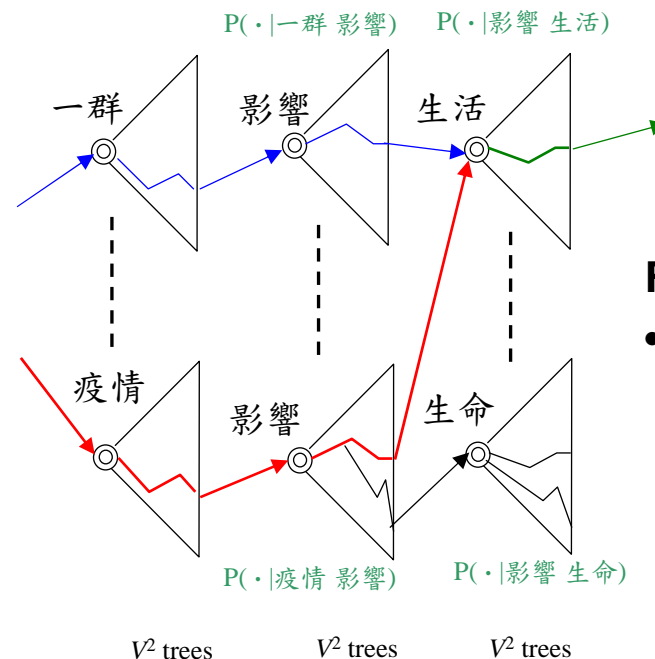


Lexical/Phonetic Tree

- Reasons for using the lexical/phonetic tree
 - States according to phones that are common to different words are shared by different hypotheses
 - A compact representation of the acoustic-phonetic search space
 - The uncertainty about the word identity is much higher at its beginning than its beginning
 - More computations required at the beginning of a word than toward its end

One-Pass Tree-Copy Search

- Word (history)-conditioned Search
 - **A virtual/imaginary tree copy** explored for linguistic context of active search hypotheses
 - Search hypotheses recombined at tree root nodes according to language modeling (or the history)



For n-gram language modeling:

- Retain distinct n-1-gram word histories

One-Pass Tree-Copy Search

- Integration of **acoustic** and **linguistic** knowledge
 - A network (**dynamically**) built to describe sentences in terms of words
 - Language models for network transition probabilities
 - A network (**statically**) built to describe words in terms of phone
 - The pronunciation dictionary (organized as a phonetic tree)
 - Transition penalties are applied
 - A network (**statically**) built to describe a phone unit in terms of sequences of HMM states
 - Spectral vectors derived from the speech signal are consumed

One-Pass Tree-Copy Search

- Three basic operations performed

- Acoustic-level recombinations within tree arcs

- Viterbi search

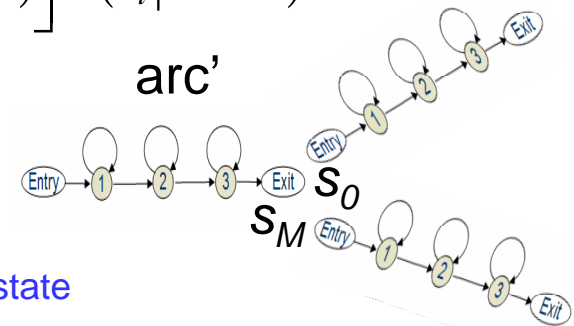
$$Q_{v_1^{n-1}}(t, s; arc) = \max_{s'} \left[Q_{v_1^{n-1}}(t-1, s'; arc) P(s|s'; arc) \right] P(x_t | s; arc) \quad \text{arc}$$

Backtracking
Information
should be
manipulated

- Tree arc extensions

$$Q_{v_1^{n-1}}(t, S_0; arc) = Q_{v_1^{n-1}}(t-1, S_M; arc')$$

↖ The beginning state
↖ The ending state



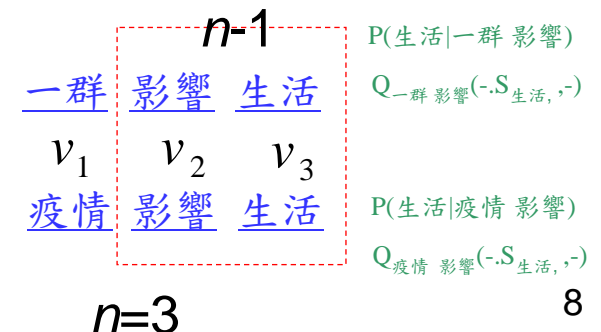
- Language-model-level recombination

- Word end hypotheses sharing the same history were recombined

$$H(v_2^n; t) = \max_{v_1} \left[Q_{v_1^{n-1}}(t, S_{v_n}; arc_E) \cdot P(v_n | v_1^{n-1})^\alpha \right]$$

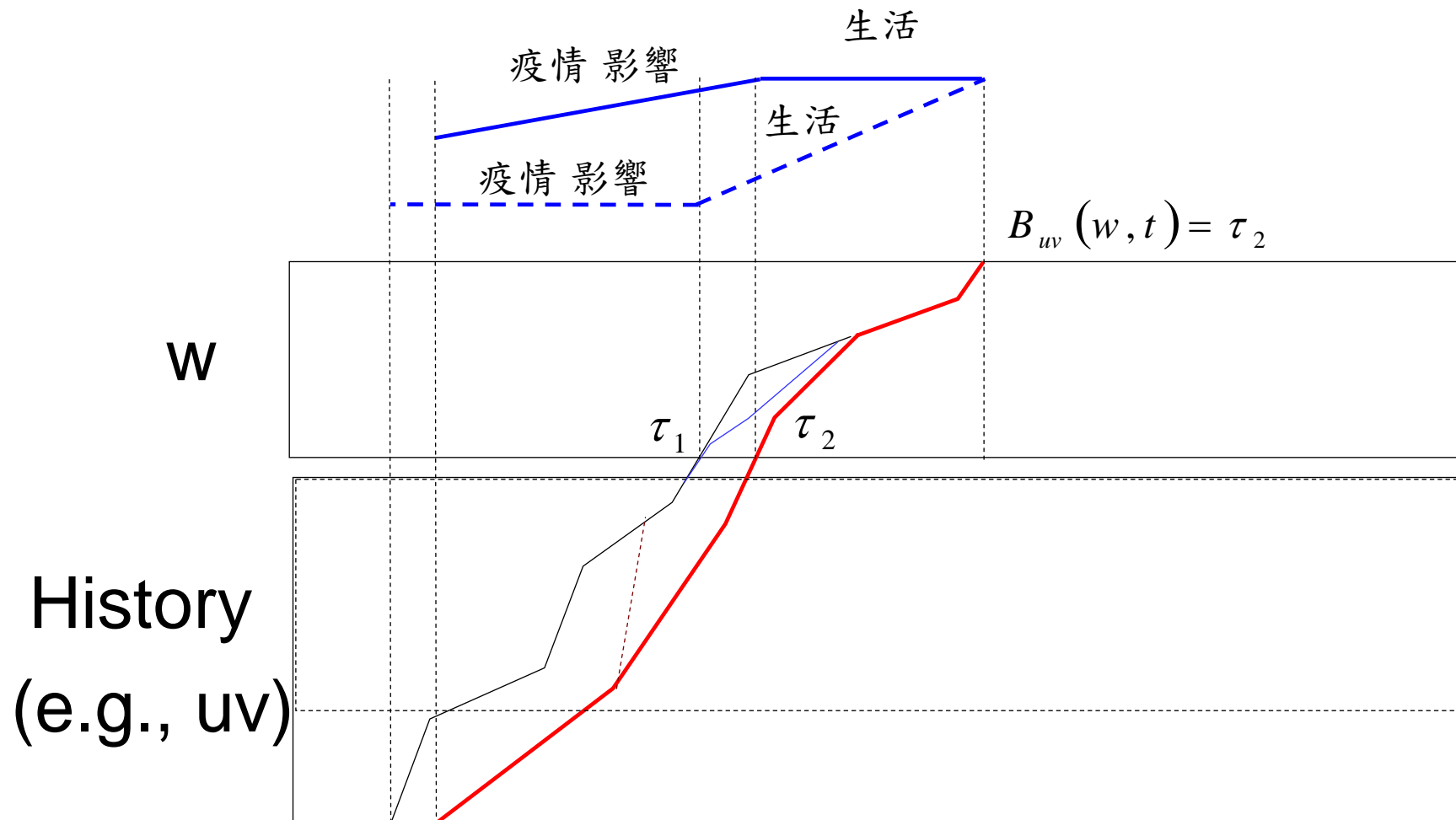
$$Q_{v_2^n}(t, S_0; arc_B) = H(v_2^n; t)$$

$$Q_{v_1^{n-1}}(t, S_0; arc_B)$$



One-Pass Tree-Copy Search

- Acoustic-level recombinations



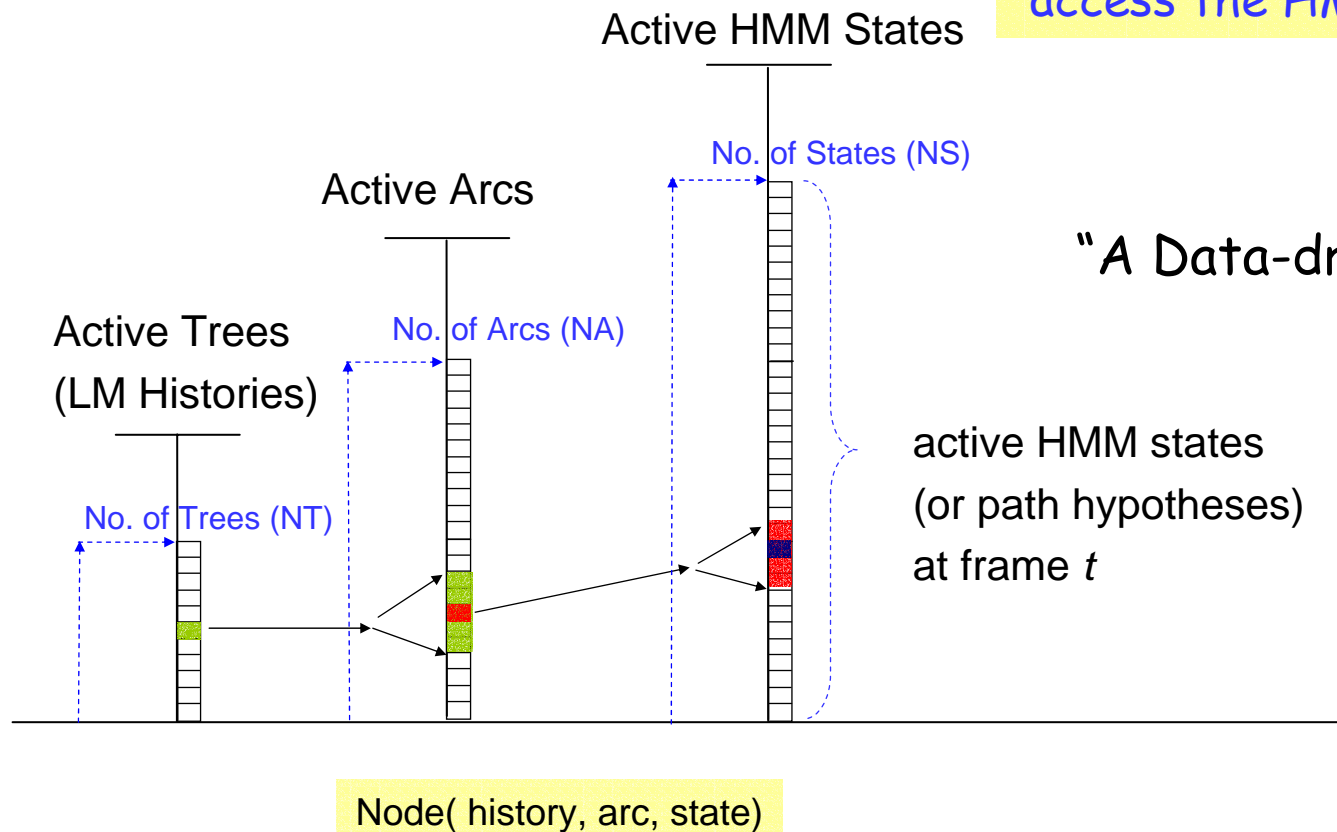
One-Pass Tree-Copy Search

- Different path hypotheses at each time frame are differentiated based on
 - The N-1 word history (for the N-gram LM)
 - The phone unit (or the tree arc)
 - The HMM state

One-Pass Tree-Copy Search

- Organization of active search hypotheses (states)
 - Hierarchical organization

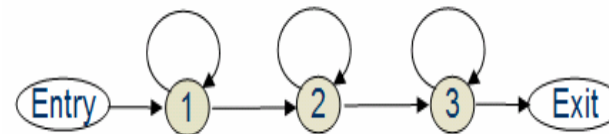
How to directly and efficiently access the HMM states ?



"A Data-driven Approach"

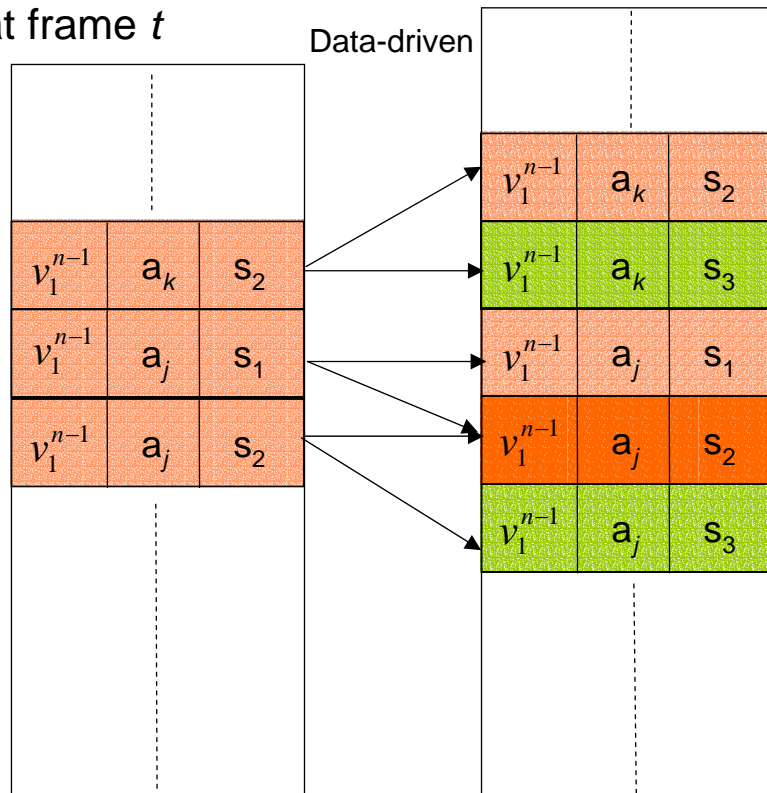
One-Pass Tree-Copy Search

- Organization of active search hypotheses (states)
 - Flat organization



Active HMM States
at frame t

New HMM States
at frame $t+1$



Acoustic level recombination

$$Q_{v_1^{n-1}}(t, s; arc) = \max_{s'} \left[Q_{v_1^{n-1}}(t-1, s'; arc) P(s|s'; arc) \right] P(x_t|s; arc)$$

C++ STL (Standard Template Libraries) is suitable for such an organization

$\log(NS)$ for the access of any HMM state

NS: the number of HMM states

One-Pass Tree-Copy Search

- Viterbi search
 - Belong to a class of breadth-first search
 - *Time-synchronous*
 - Hypotheses terminate at the same point in time
 - Therefore, hypotheses can be compared
 - The search hypotheses will grow *exponentially*
 - Pruning away unlikely (incorrect) paths is needed
 - Viterbi *beam* search
 - Hypotheses with likelihood falling within a fixed radius (or beam) of the most likely hypothesis are retained
 - The beam size determined empirically or adaptively

One-Pass Tree-Copy Search

- Pruning Techniques

- Standard Beam Pruning (Acoustic-level Pruning)

- Retain only hypotheses with a score close to the best hypothesis

$$Thr_{AC}(t) = \left[\max_{(v_1^{n-1}, s, arc)} Q_{v_1^{n-1}}(t, s; arc) \right] \times f_{AC}$$

$$Q_{v_1^{n-1}}(t, s; arc) < Thr_{AC}(t) \Rightarrow \text{pruned!}$$

- Language Model Pruning (word-level Pruning)

- Applied to word-end or tree start-up hypotheses

$$Thr_{LM}(t) = \left[\max_{(v_1^{n-1}, S_0, arc_B)} Q_{v_1^{n-1}}(t, S_0; arc_B) \right] \times f_{LM}$$

$$Q_{v_1^{n-1}}(t, S_0; arc_B) < Thr_{LM}(t) \Rightarrow \text{pruned!}$$

- Histogram Pruning

- Limit the number of surviving state hypotheses to a maximum number (Need some kind of sorting!)
- **Not Recommended!**

One-Pass Tree-Copy Search

- Pruning Techniques (cont.)
 - Stricter pruning applied at word ends
 - The threshold is tightly compared to the acoustic-level one
 - **Reasons**
 - A single path hypothesis is propagated into multiple word ends (同音詞問題)
 - A large number of arcs (models) of the new generated tree copies are about to be activated

Pose severe
requirements on
the system memory

One-Pass Tree-Copy Search

- Pruning techniques in my system

```
Acoustic_Penalty=800;
Acoustic_MAX=(float) Min_Delta;
count=0;
for(state_no=0;state_no<NewTreeState;state_no++)
{
    cur_HMM=LEX_STATE[PT2][state_no].TPTR->Model_ID;
    cur_state=LEX_STATE[PT2][state_no].HMM_state;
    if(LEX_STATE[PT2][state_no].Score>Acoustic_MAX)
        Acoustic_MAX=LEX_STATE[PT2][state_no].Score;
}
for(state_no=0;state_no<NewTreeState;state_no++)
{
    cur_HMM=LEX_STATE[PT2][state_no].TPTR->Model_ID;
    cur_state=LEX_STATE[PT2][state_no].HMM_state;
    if(LEX_STATE[PT2][state_no].Score>(Acoustic_MAX-Acoustic_Penalty))
        count++;
}
//20020522
if(count>100000)    Acoustic_MAX=Acoustic_MAX-40;
else if(count>50000) Acoustic_MAX=Acoustic_MAX-80;
else if(count>10000) Acoustic_MAX=Acoustic_MAX-100;
else if(count>5000)  Acoustic_MAX=Acoustic_MAX-150;
else if(count>2000)  Acoustic_MAX=Acoustic_MAX-200;
else if(count>1000)  Acoustic_MAX=Acoustic_MAX-300;
else if(count>400)   Acoustic_MAX=Acoustic_MAX-400;
else                 Acoustic_MAX=Acoustic_MAX-500;
ATreeState=0;
for(state_no=0;state_no<NewTreeState;state_no++)
{
    if(LEX_STATE[PT2][state_no].Score>Acoustic_MAX)
    {
        LEX_STATE[PT1][ATreeState]=LEX_STATE[PT2][state_no];
        ATreeState++;
    }
}
```

Acoustic-Level Pruning

One-Pass Tree-Copy Search

- Pruning techniques in my system

Word-Level Pruning

```
LM_Penalty=200;
LM_MAX=(float) Min_Delta;
for(j=0;j<LOCAL_ACTIVE_WORD_NO;j++)
    if(LOCAL_ACTIVE_TREE[j].Score>LM_MAX)
        LM_MAX=LOCAL_ACTIVE_TREE[j].Score;

count=0;
for(j=0;j<LOCAL_ACTIVE_WORD_NO;j++)
    if(LOCAL_ACTIVE_TREE[j].Score>(LM_MAX-LM_Penalty))
        count++;
//before 20020522
if (count>200) LM_MAX=LM_MAX-30;
else if(count>100) LM_MAX=LM_MAX-50;
else if(count>50) LM_MAX=LM_MAX-70;
else
    LM_MAX=LM_MAX-80;

count=0;
for(j=0;j<LOCAL_ACTIVE_WORD_NO;j++)
    if(LOCAL_ACTIVE_TREE[j].Score>=LM_MAX)
        count++;

if((ACTIVE_TREE_WORD[Frame_Num]
    =( struct DEF_ACTIVE_TREE_WORD *)malloc((count+1)*sizeof( struct DEF_ACTIVE_TREE_WORD)))==NULL)
{
    printf("ACTIVE_TREE_WORD allocation error at FRAME %d!\n",Frame_Num);
    exit(1);
}

ACTIVE_TREE_WORD_NO[Frame_Num]=0;
for(j=0;j<LOCAL_ACTIVE_WORD_NO;j++)
    if(LOCAL_ACTIVE_TREE[j].Score>=LM_MAX)
    {
        ACTIVE_TREE_WORD[Frame_Num][ACTIVE_TREE_WORD_NO[Frame_Num]]=LOCAL_ACTIVE_TREE[j];
        ACTIVE_TREE_WORD_NO[Frame_Num]++;
    }
}
```

One-Pass Tree-Copy Search

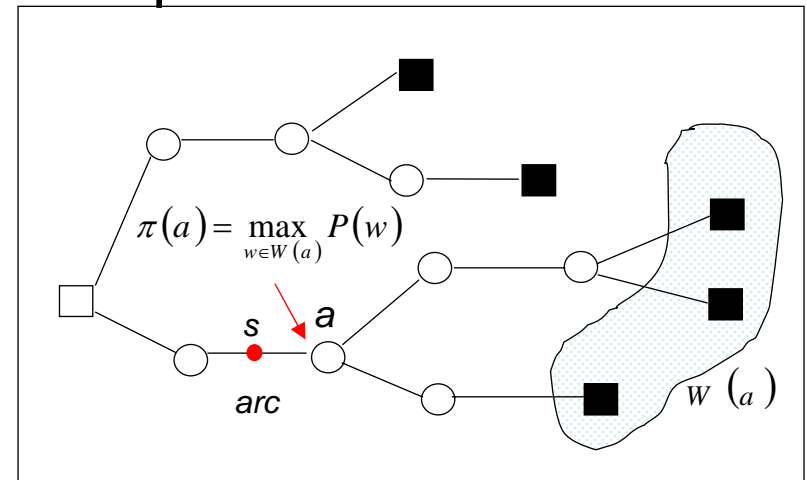
- Language Model Look-ahead
 - Language model probabilities incorporated as early in the search as possible
 - Language model probability incorporated for computing of $Q_{v_1^{n-1}}(t, s; arc)$

- Unigram Look-ahead

$$\pi(a) = \max_{w \in W(a)} P(w)$$

- Bigram Look-ahead

$$\pi_v(a) = \max_{w \in W(a)} P(w|v)$$



- Anticipate the language model probabilities with the state hypothesis

$$\tilde{Q}_{v_1^{n-1}}(t, s; arc) = \pi(a_{s, arc}) Q_{v_1^{n-1}}(t, s; arc)$$

$$\tilde{Q}_{v_1^{n-1}}(t, s; arc) < \overline{Thr}_{AC}(t) \Rightarrow \text{pruned!}$$

$$\overline{Thr}_{AC}(t) = \left[\max_{(v_1^{n-1}, s, arc)} \pi(a_{s, arc}) Q_{v_1^{n-1}}(t, s; arc) \right] \times f_{AC}$$

One-Pass Tree-Copy Search

- Language Model Look-ahead

```
void SpeechClass::Calculate_Word_Tree_Unigram()  
{  
    if(Root==(struct Tree *) NULL) return;  
    Do_Calculate_Word_Tree_Unigram(Root);  
}
```

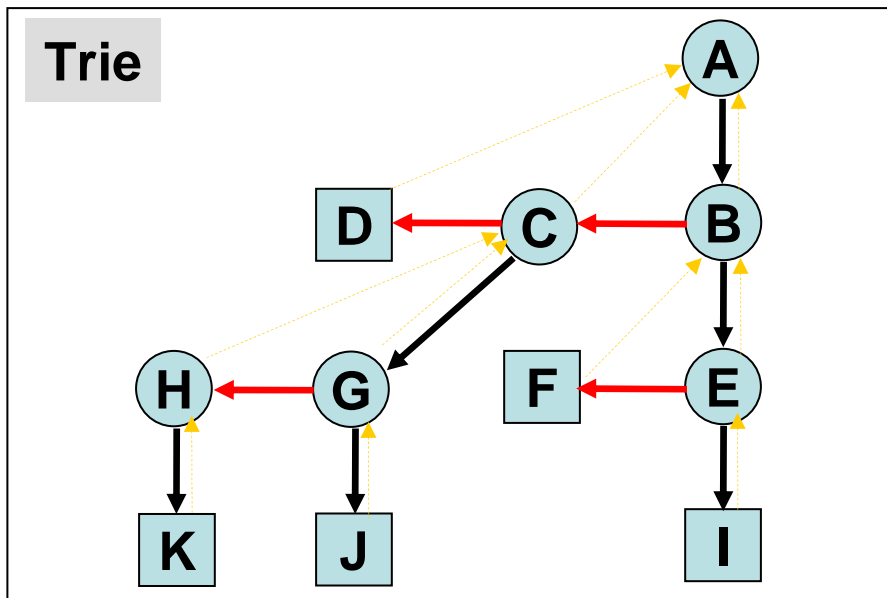
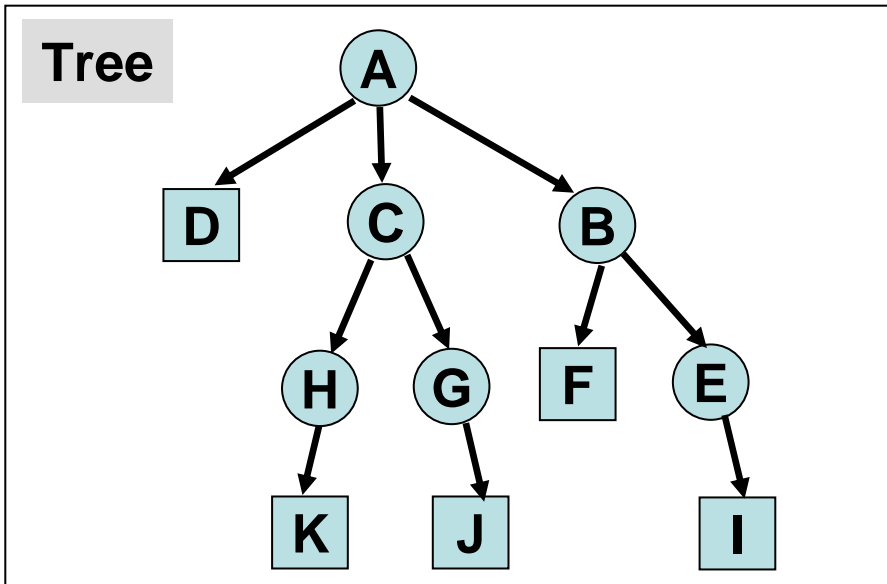
Recursive function for
calculating unigram LM
look-ahead

```
void SpeechClass::Do_Calculate_Word_Tree_Unigram(struct Tree *ptrNow)  
{  
    if(ptrNow==(struct Tree *) NULL) return;  
    Do_Calculate_Word_Tree_Unigram(ptrNow->Brother);  
    Do_Calculate_Word_Tree_Unigram(ptrNow->Child);  
    if(ptrNow->Father!=(struct Tree *) NULL)  
        if(ptrNow->Unigram > ptrNow->Father->Unigram)  
            ptrNow->Father->Unigram=ptrNow->Unigram;  
}
```

One-Pass Tree-Copy Search

- Trie Structure

```
struct DEF_LEXICON_TREE
{
    short   Model_ID;
    short   WD_NO;
    int     *WD_ID;
    int     Leaf;
    double  Unigram;
    struct  Tree *Child;
    struct  Tree *Brother;
    struct  Tree *Father;
};
```



One-Pass Tree-Copy Search

- **Linear Lexicon** with Bigram Language Modeling

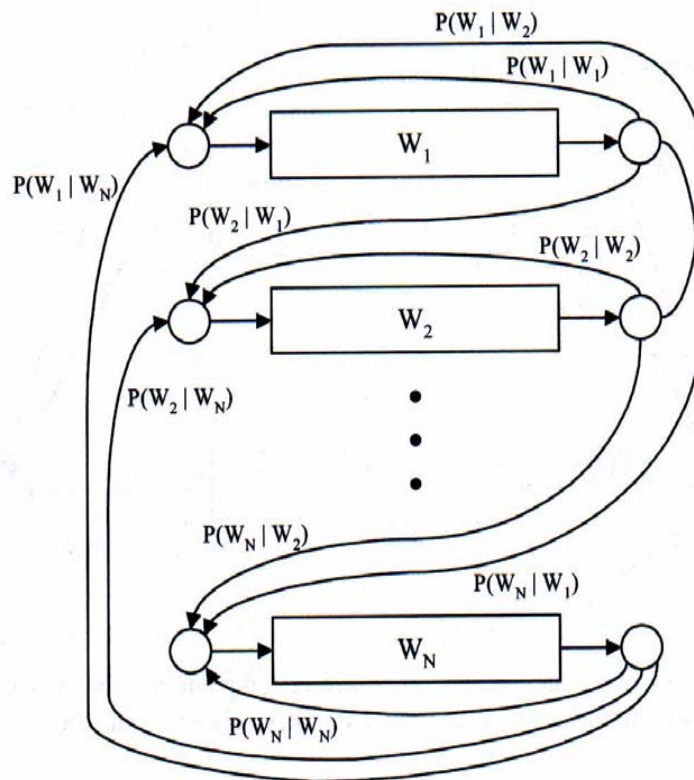


Figure 12.15 A bigram grammar network where the bigram probability $P(w_j | w_i)$ is attached as the transition probability from word w_i to w_j [19].

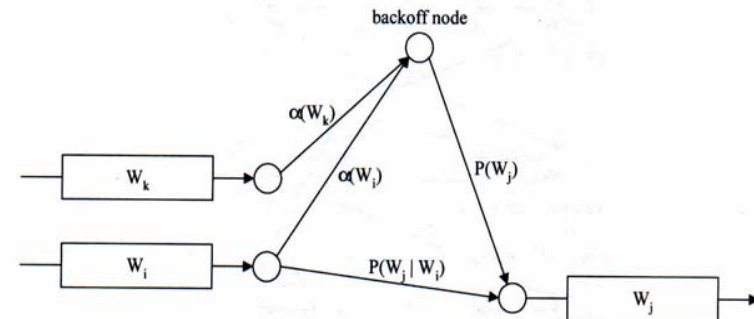
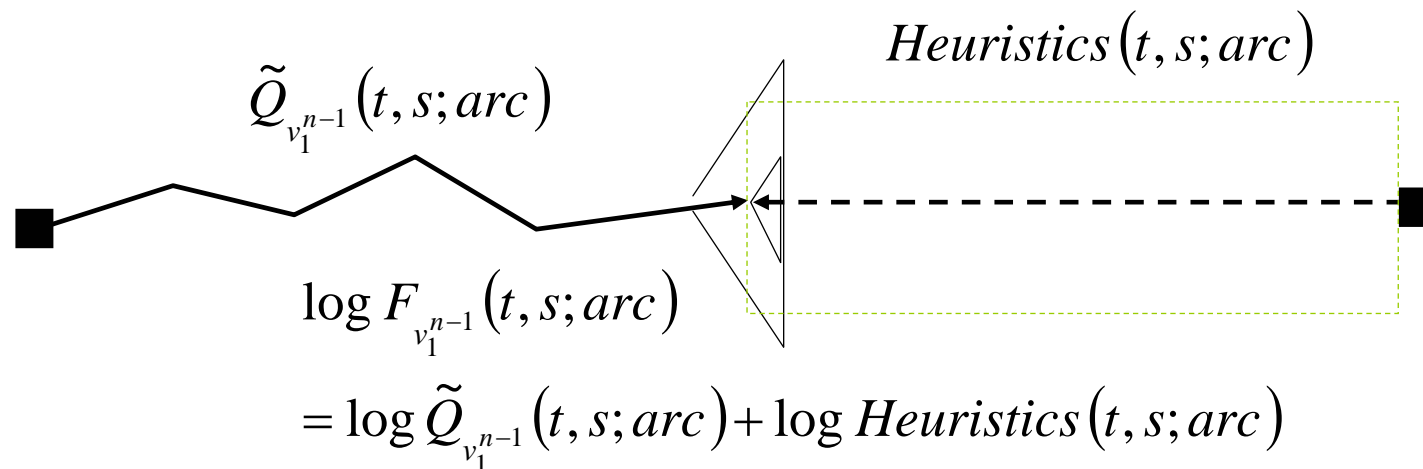


Figure 12.16 Reducing bigram expansion in a search by using the backoff node. In addition to normal bigram expansion arcs for all observed bigrams, the last state of word w_i is first connected to a central backoff node with transition probability equal to backoff weight $\alpha(w_i)$. The backoff node is then connected to the beginning of each word w_j with its corresponding unigram probability $P(w_j)$ [12].

One-Pass Tree-Copy Search

- Acoustic Look-ahead
 - The same idea from A* search
 - The use of acoustic heuristics to speed up the search process
 - Help to make the right decision when pruning
 - How to design the procedure in order to estimate the heuristics ?



Word Graph

- If **bigram LM** used in the tree-copy search
 - The beginning time of a word hypothesis w ending at time t

$$\tau(t; v, w) = B_v(t, S_w; arc_E)$$

- The acoustic score of a word hypothesis w

$$AC_v(w; \tau, t) = Q_v(t, S_{v_n}; arc_E) / H(v, \tau)$$

Not only the word hypothesis with
the best predecessor word were recorded

$$AC_{v_0}(w; \tau_0, t)$$

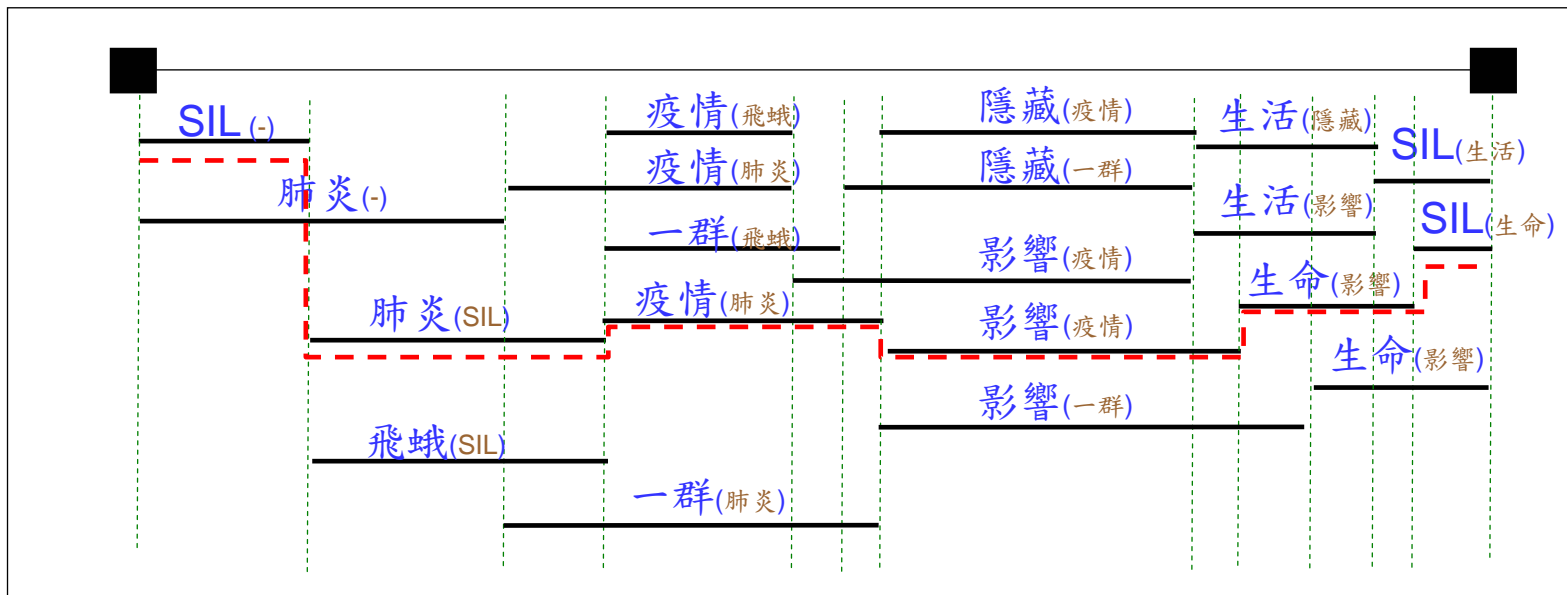
$$AC_{v_1}(w; \tau_1, t)$$

$$AC_{v_2}(w; \tau_2, t)$$

⋮

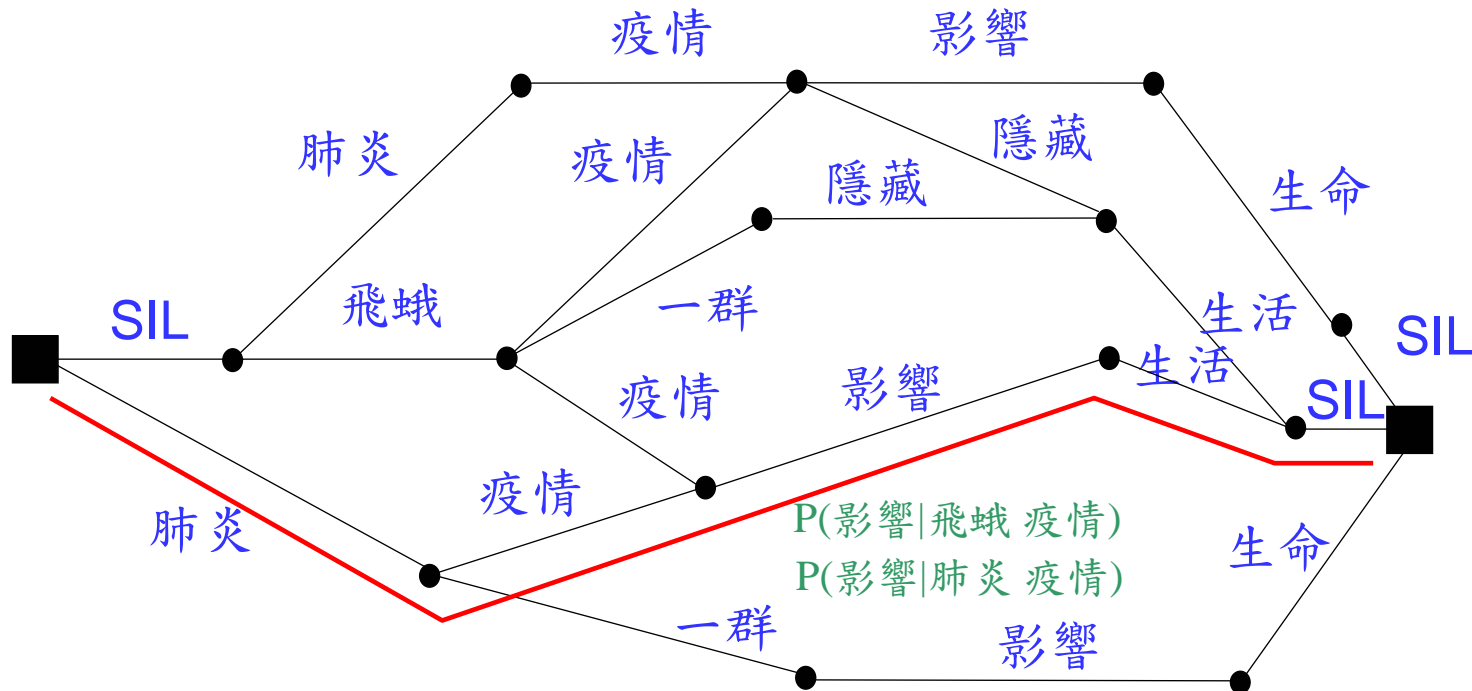
Word Graph

- Bookkeeping at the word level
 - When word hypotheses were recombined into one hypothesis to start up the next tree
 - Not only the word hypothesis with the best predecessor word were recorded
 - But for the hypotheses that have the same LM history, only the best one was kept



Word Graph

- A word graph built with word-pair approximation



- Each edge stands for a word hypothesis
- The node at the right side of an edge denotes the **word end**
 - There is a maximum of incoming word edges for a node (?)
 - There is no maximum of the num. of outgoing edges for a node (?)

One-Pass Tree-Copy Search

- Time-Conditioned Search

- Acoustic-level recombinations within tree arcs

- Viterbi search

$$Q_\tau(t, s; arc) = \max_{s'} [Q_\tau(t-1, s'; arc) P(s|s'; arc)] P(x_t|s; arc)$$

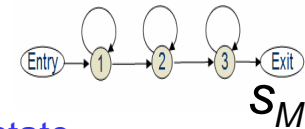
The starting time of the lexical tree

- Tree arc extensions

$$Q_\tau(t, S_0; arc) = Q_\tau(t-1, S_M; arc')$$

The beginning state

The ending state



- Language-model-level recombination

- Word end hypotheses sharing the same history were recombined

$$h(v_n; \tau, t) = Q_\tau(t, S_{v_n}; arc_E) / H_{\max}(\tau)$$

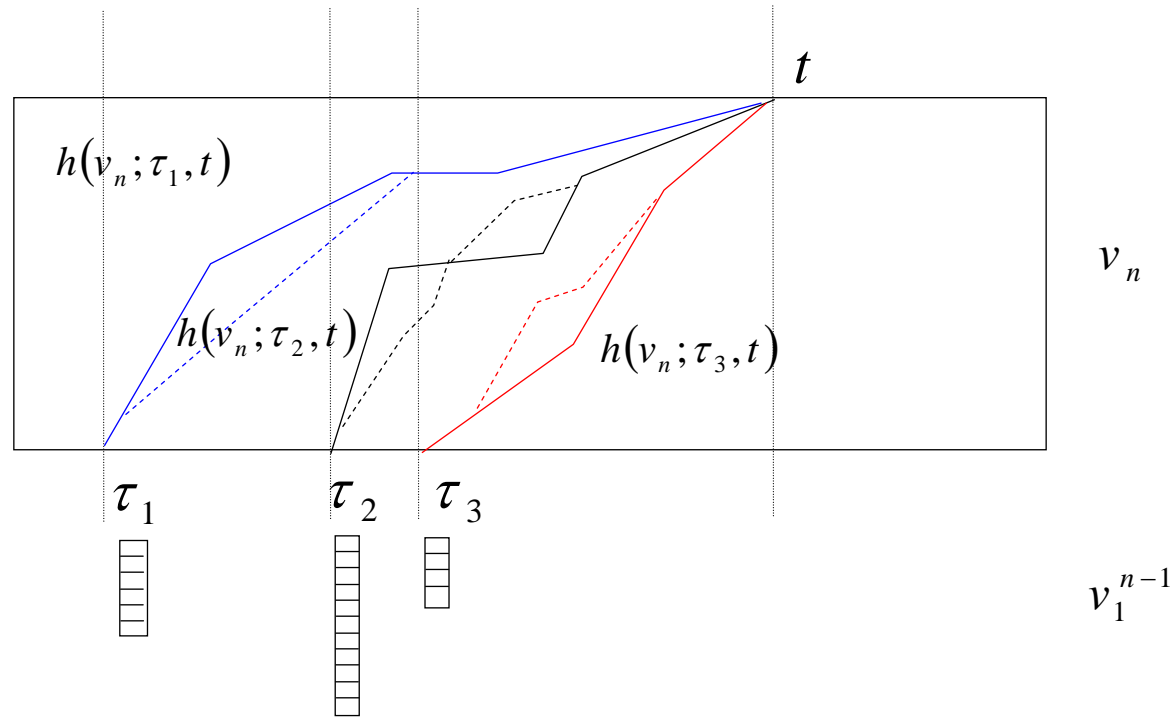
$$H(v_2^n; t) = \max_{(v_1, \tau)} \left[H(v_1^{n-1}; \tau) \cdot h(v_n; \tau, t) \cdot P(v_n | v_1^{n-1})^\alpha \right]$$

$$H_{\max}(t) = \max_{v_2^n} H(v_2^n; t)$$

$$Q_t(t, S_0; arc_B) = H_{\max}(t)$$

One-Pass Tree-Copy Search

- Time-Conditioned Search



$$\begin{aligned}
 H(v_2^n; t) &= \max_{(v_1, \tau)} \left[H(v_1^{n-1}; \tau) \cdot h(v_n; \tau, t) \cdot P(v_n | v_1^{n-1})^\alpha \right] \\
 &= \max_{(v_1, \tau)} \left[H(v_1^{n-1}; \tau) \cdot \frac{Q_\tau(t, S_{v_n}; \text{arc}_E)}{H_{\max}(\tau)} \cdot P(v_n | v_1^{n-1})^\alpha \right]
 \end{aligned}$$